



# Moorside Primary School and Nursery

Progression in bar modelling



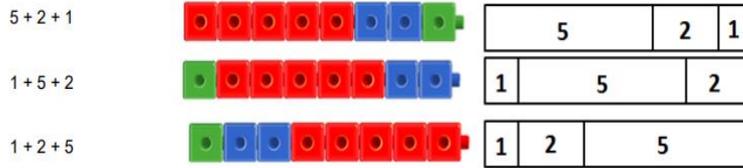
Bar models are pictorial representations of problems or concepts that can be used for any of the 4 main operations. They are also very helpful for fractions, percentages and ratio and proportion. In word problems bar models can help children to decide which operations to use or to visualise problems.

The main aim of a bar model is to give a pictorial representation of the underlying structure of a mathematical problem. As a result, this helps children understand and solve the problem as it exposes the mathematical concept allowing children to easily understand what calculation to perform.

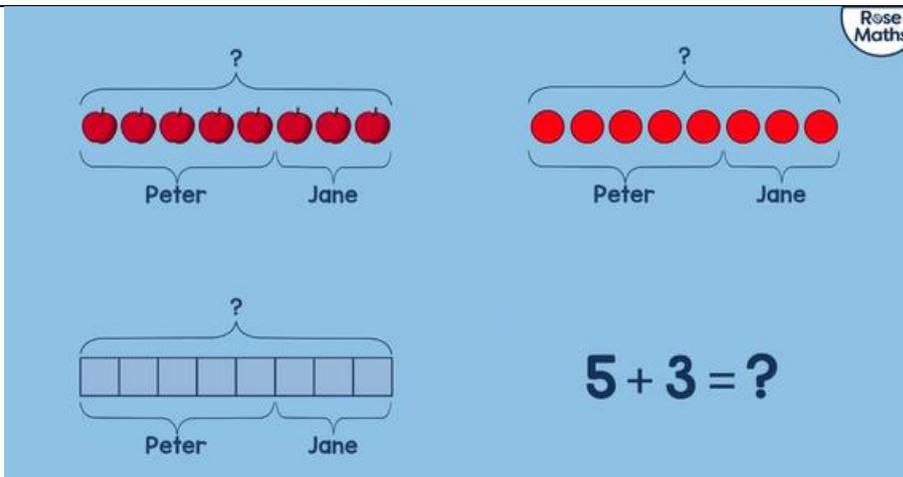
The next pages outline how we progressively teach bar modelling at Moorside Primary School and Nursery.

# ADDITION

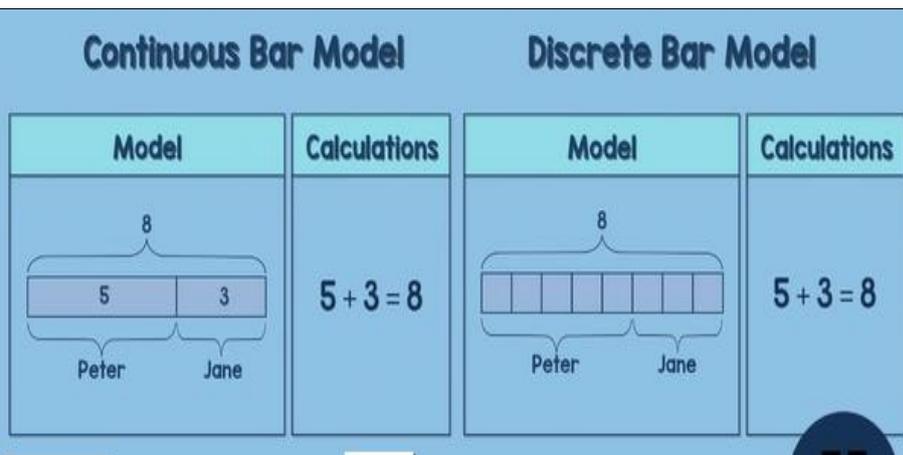
Exploring commutativity and associative law.



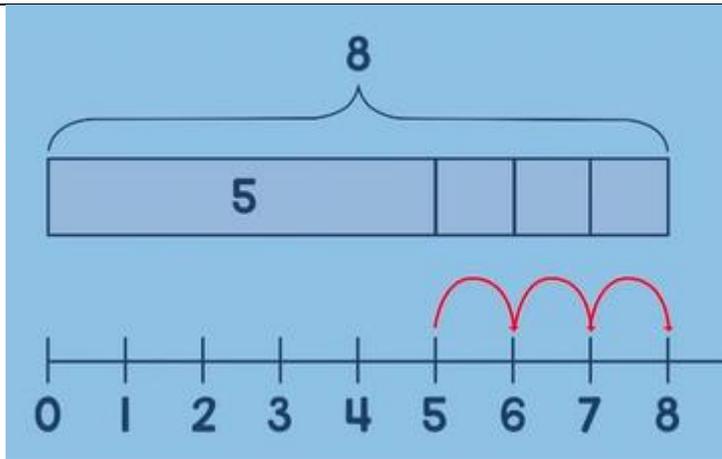
A bar model begins through a concrete representation, encouraging children to understand commutativity.



This is a discrete model which encourages children to count out. We can model this with a continuous bar model which is more efficient and encourages children to learn their number bonds.

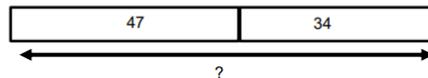
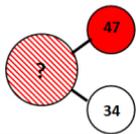


This is an example of aggregation, where two parts come together to make a whole. Eg. Peter has 5 apples. Jane has 3 apples. How many apples do they have altogether?



If children struggle and are wanting to count the individual squares, we can mix the discrete and continuous bar model so they can count on. In the example here, they are counting on from 5. This is an example of augmentation.

Amber has 47 pence and Isabel has 34 pence. How much do they have altogether?



$$81 = 34 + 47$$

$$47 + 34 = 81$$

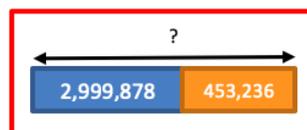
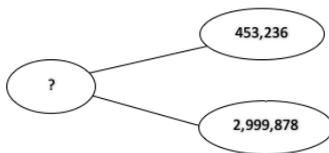
$$81 - 34 = 47$$

$$81 - 47 = 34$$

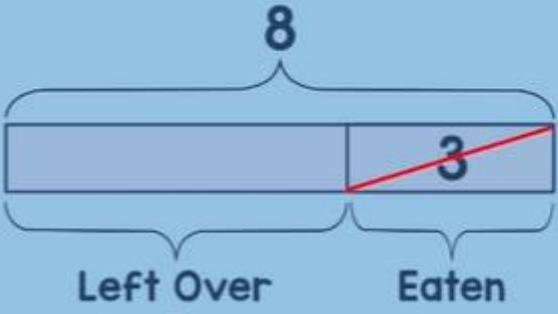
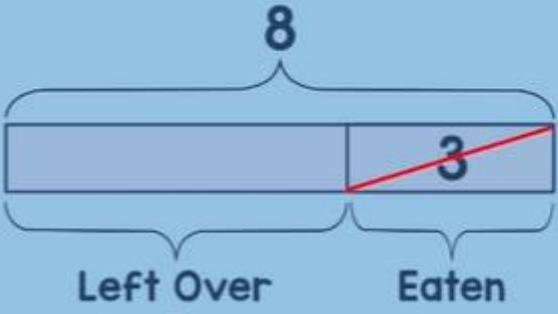
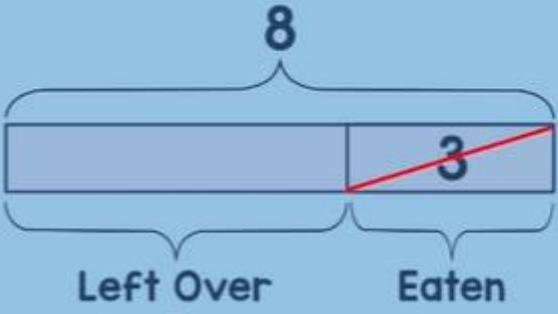
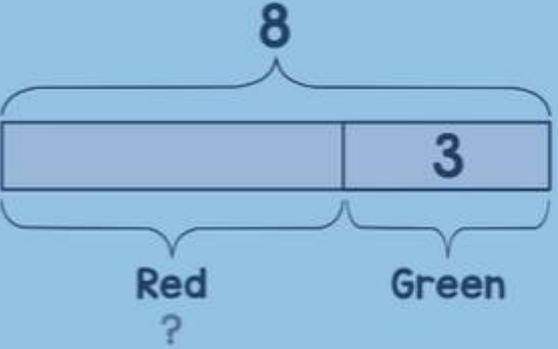
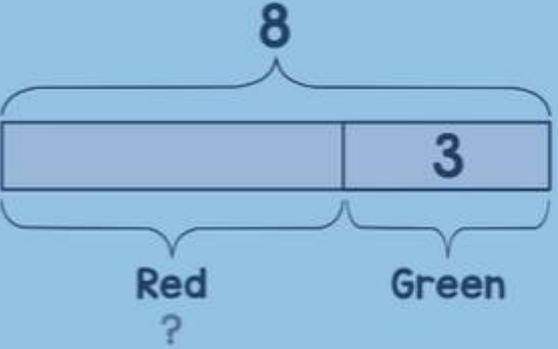
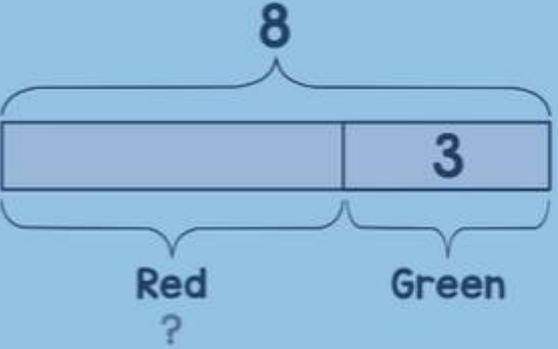
$$34 = \square - 47$$

34 more than 47 is 81.  
81 is 47 more than 34.  
47 fewer than 81 is 34.  
34 is 47 fewer than 81.

As numbers get larger, a continuous bar model supports children's understanding and links with commutativity.



# SUBTRACTION

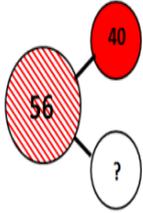
<table border="1"><thead><tr><th data-bbox="130 405 759 510">Model</th><th data-bbox="775 405 1136 510">Calculations</th></tr></thead><tbody><tr><td data-bbox="130 510 759 909"><p>8</p><p>Left Over      Eaten</p></td><td data-bbox="775 510 1136 909"><math>8 - 3 = ?</math></td></tr></tbody></table>	Model	Calculations	 <p>8</p> <p>Left Over      Eaten</p>	$8 - 3 = ?$	<p>Bar models are always shown with the calculation alongside.</p> <p>This example is called reduction.</p> <p>Jane has 8 apples, she eats 3. How many does she have left? We strike the 3 out to show what has been taken away.</p>
Model	Calculations				
 <p>8</p> <p>Left Over      Eaten</p>	$8 - 3 = ?$				
<table border="1"><thead><tr><th data-bbox="130 1025 759 1131">Model</th><th data-bbox="775 1025 1136 1131">Calculations</th></tr></thead><tbody><tr><td data-bbox="130 1131 759 1581"><p>8</p><p>Red ?      Green</p></td><td data-bbox="775 1131 1136 1581"><math>8 - 3 = ?</math></td></tr></tbody></table>	Model	Calculations	 <p>8</p> <p>Red ?      Green</p>	$8 - 3 = ?$	<p>This example is called partitioning.</p> <p>Jane has 8 apples. There are 3 green apples and the rest are red. How many apples are red?</p>
Model	Calculations				
 <p>8</p> <p>Red ?      Green</p>	$8 - 3 = ?$				

Model	Calculations
Peter <span style="border: 1px solid black; padding: 2px 10px;">8</span>  Jane <span style="border: 1px solid black; padding: 2px 10px;">3</span> <span style="color: red; font-size: 1.2em;">→ 5</span>	$8 - 3 = 5$

To model a difference question, we use a comparison bar model.

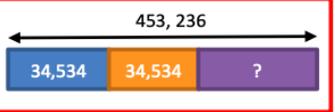
Peter has 8 apples.  
Jane has 3 apples.  
How many more apples does Peter have than Jane?

*Amber has 40 buttons. Isabel has 56 buttons. How many fewer buttons does Amber have than Isabel?*



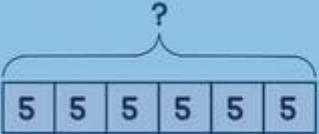
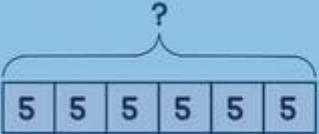
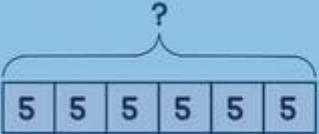
Isabel	56
Amber	40

Bar models are used to support the understanding of more complex problems involving subtraction.

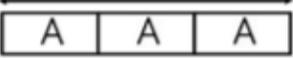
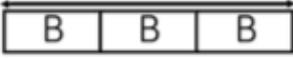


James needs 34,534 bricks to build a mansion.  
He buys 7,784 and has 3,698 left over from another job. How many more does he need?

# MULTIPLICATION

<table border="1" style="width: 100%; border-collapse: collapse; background-color: #e0f0ff;"> <thead> <tr> <th style="width: 50%; padding: 5px;">Model</th> <th style="width: 50%; padding: 5px;">Calculations</th> </tr> </thead> <tbody> <tr> <td style="padding: 10px; text-align: center;">  </td> <td style="padding: 10px; text-align: center;"> <math>6 \times 5 = ?</math> </td> </tr> </tbody> </table>	Model	Calculations		$6 \times 5 = ?$	<p>Muffins come in boxes of 5. Peter buys 6 boxes of muffins. How many muffins did Peter buy altogether?</p> <p>This shows the connection between multiplication and repeated addition.</p>									
Model	Calculations													
	$6 \times 5 = ?$													
<table border="1" style="width: 100%; border-collapse: collapse; background-color: #e0f0ff;"> <thead> <tr> <th style="width: 50%; padding: 5px;">Model</th> <th style="width: 50%; padding: 5px;">Calculations</th> </tr> </thead> <tbody> <tr> <td style="padding: 10px; text-align: center;">  </td> <td style="padding: 10px; text-align: center;"> <math>6 \times 5 = 30</math>  <math>5 \times 6 = 30</math> </td> </tr> </tbody> </table>	Model	Calculations		$6 \times 5 = 30$ $5 \times 6 = 30$	<p>The bar model shows how multiplication is commutative.</p>									
Model	Calculations													
	$6 \times 5 = 30$ $5 \times 6 = 30$													
<p><b>Multiplication and Division</b></p> <p>1. Kate bought 4 blouses for £89 each and 2 similar pair of jeans. She paid £574. Find the cost of 1 pair of jeans.</p> <table style="margin-left: 20px;"> <tr> <td style="border: 1px solid black; padding: 2px;">Blouse</td> <td style="border: 1px solid black; padding: 2px; width: 40px;">£89</td> <td style="border: 1px solid black; padding: 2px; width: 40px;">£89</td> <td style="border: 1px solid black; padding: 2px; width: 40px;">£89</td> <td style="border: 1px solid black; padding: 2px; width: 40px;">£89</td> <td rowspan="2" style="font-size: 2em; padding-left: 10px;">}</td> <td rowspan="2" style="vertical-align: middle;">574</td> </tr> <tr> <td style="border: 1px solid black; padding: 2px;">Jeans</td> <td style="border: 1px solid black; padding: 2px; width: 40px;">?</td> <td style="border: 1px solid black; padding: 2px; width: 40px;">?</td> <td colspan="3"></td> </tr> </table> <p style="margin-left: 20px;"><i>From the bar model above, we know that</i></p> <p style="margin-left: 20px;">4 blouse cost = £89 x 4 = £356</p> <p style="margin-left: 20px;">2 pair of jeans cost = £574 - £356 = £218</p> <p style="margin-left: 20px;">1 pair of jeans will cost = £218 ÷ 2 = <b>£109</b></p>	Blouse	£89	£89	£89	£89	}	574	Jeans	?	?				<p>Bar models are used to support the understanding of multi-step problems involving multiplication and division.</p>
Blouse	£89	£89	£89	£89	}			574						
Jeans	?	?												

# DIVISION

<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="background-color: #ADD8E6; text-align: center;">Model</th> <th style="background-color: #ADD8E6; text-align: center;">Calculations</th> </tr> </thead> <tbody> <tr> <td style="text-align: center;"> <div style="margin-bottom: 10px;">30</div>  <p style="margin-top: 10px;">Number of cakes in each box = 6</p> </td> <td style="text-align: center; vertical-align: middle;"> <math>30 \div 5 = 6</math> </td> </tr> </tbody> </table>	Model	Calculations	<div style="margin-bottom: 10px;">30</div>  <p style="margin-top: 10px;">Number of cakes in each box = 6</p>	$30 \div 5 = 6$	<p style="text-align: center;"><b>Sharing</b></p> <p>Jane has 30 cakes. She wants to share them equally between 5 boxes. How many should go in each box?</p>
Model	Calculations				
<div style="margin-bottom: 10px;">30</div>  <p style="margin-top: 10px;">Number of cakes in each box = 6</p>	$30 \div 5 = 6$				
<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="background-color: #ADD8E6; text-align: center;">Model</th> <th style="background-color: #ADD8E6; text-align: center;">Calculations</th> </tr> </thead> <tbody> <tr> <td style="text-align: center;"> <div style="margin-bottom: 10px;">30</div>  </td> <td style="text-align: center; vertical-align: middle;"> <math>30 \div 5 = ?</math> </td> </tr> </tbody> </table>	Model	Calculations	<div style="margin-bottom: 10px;">30</div> 	$30 \div 5 = ?$	<p style="text-align: center;"><b>Grouping</b></p> <p>Jane has 30 cakes. She wants to pack them into boxes with 5 cakes in each box. How many boxes will she need?</p>
Model	Calculations				
<div style="margin-bottom: 10px;">30</div> 	$30 \div 5 = ?$				
<p>Work out the value of C. (The bar models are not drawn to scale)</p> <div style="margin: 10px 0;"> <math>4,950</math>   </div> <div style="margin: 10px 0;"> <math>A</math>   </div> <div style="margin: 10px 0;"> <math>B</math>   </div>	<p>Bar models are used to demonstrate multi-step problems involving division.</p>				

